George D. Birkhoff

GEORGE D. BIRKHOFF

Nato il 21 marzo 1884 ad Overisel (Michigan) da David e Zane Gertrude Droppers. Professore di Matematica nella Harvard University di Cambridge, Mass. (U. S. A.). Accademico Pontificio dal 28 ottobre 1936.

Studiò a Chicago ed in quell'Università si addottorò nel 1907 in Filosofia. In precedenza (1905, 1906) aveva ottenuto all'Università di Harvard i gradi A. B. ed A. M. Dal 1907 al 1909 insegnò Matematica all'Università del Wisconsin, dal 1909 al 1911 fu professore straordinario di Matematica all'Università di Princeton e nel 1911-1912 fu ordinario nella stessa Università. Nel 1912 passò all'Università di Harvard ove fu straordinario fino al 1919, ordinario 1919-1933; dal 1933 è Perkins Professor. Nel 1935 fu nominato decano della facoltà di Arti e Scienze all'Università di Harvard. Nel 1930 tenne un corso al Collège de France.

Per varie volte fu direttore di riviste matematiche degli Stati Uniti.

È dottore *honoris causa*: della Brown University (Presidence, R. I., 1923), della Università del Wisconsin (Madison 1927), della Harvard (Cambridge, Mass., 1933), nonchè delle Università di Poitiers (1933) e di Parigi (1936).

È membro (ordinario, corrispondente od onorario) delle seguenti Accademie: National Academy of Sciences; American Philosophical Society; American Academy of Arts and Sciences; Ame-

rican Mathematical Society (Presidente dal 1924 al 1926); Circolo Matematico di Palermo; Royal Danish Academy of Sciences and Letters; Göttingen Gesellschaft der Wisseuschaften; Institut de France; Reale Accademia dei Lincei; Reale Istituto di Bologna; Edinburgh Mathematical Society.

Nel 1918 il Reale Istituto di Scienze, Lettere ed Arti di Venezia gli conferiva il premio Querini-Stampalia; nel 1923 ottenne il premio Bôcher della Società Matematica Americana per ricerche sulla dinamica; nel 1926 il premio annuale dell'Associazione Americana per il Progresso delle Scienze e nel 1933 il premio del concorso bandito dalla Pontificia Accademia delle Scienze « I Nuovi Lincei » per ricerche sui sistemi di equazioni differenziali.

È Ufficiale della Legione d'Onore (1936).

INDIRIZZO :

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PUBBLICAZIONI

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